

# Axiomatic Information Retrieval Experimentation

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# Axiomatic Information Retrieval Experimentation

- Axiomatic Constraints for Retrieval Models
  - Levels of Evaluation
  - Properties of Retrieval Models
  - Axiomatic Framework for IR
  - Practical Considerations
- Applications for Retrieval Axioms
- Hands-on: Axiomatic Experiments with `ir_axioms`
- Open Topics and Discussion

# Axiomatic Constraints for Retrieval Models

## Analogy: Levels of Software Testing

Goal: Check if software works as expected

- System tests
  - End-to-end user interaction, complete system
  - Macroscopic
- ⋮ Integration tests: part of system, no user, mesoscopic
- Unit tests
  - Lightweight, single component
  - Microscopic

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  - Microscopic: **cheap**, **limited scope**

Choose the right tool for the job!



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## Analogy: Levels of Retrieval Evaluation

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### 💻 Online Evaluation

- Example: A/B testing
- Macroscopic

### ⋮ Offline Evaluation

- Example: nDCG
- Mesoscopic

### JUnit

Unit tests?



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### Unit tests?



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- Example: TFC1
- Microscopic

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- But: Small changes can make them ineffective → Why?

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$$\rho_{\text{BM25}}(q, d) = \sum_{t \in q} \text{IDF}(t) \cdot \frac{\text{TF}(t, d) \cdot (k_1 + 1)}{\text{TF}(t, d) + k_1 \cdot \left(1 - b + b \cdot \frac{|d|}{\text{avgdl}}\right)}$$

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Example: Query Likelihood [Ponte and Croft, 1998]

$$\rho_{QL}(q, d) := p(q|d) = \prod_{t \in q} p(t|d) \cdot \prod_{t \notin q} (1 - p(t|d)) \quad \text{with:}$$

$$p(t|d) = \left( \frac{\text{TF}(t, d)}{|d|} \right)^{1 - R_{t,d}} \cdot \left( \frac{\sum_{d(t \in q)} \text{TF}(t, d) / |d|}{\text{DF}(t)} \right)^{R_{t,d}}$$

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# Axiomatic Constraints for Retrieval Models

Axiom Examples: TFC1 [Fang, Tao, Zhai 2004]

Property: **Term frequency**

Intuition: Higher score to document with more occurrences of query term.

Formalization: Given a single-term query  $q = \{t\}$  and two documents  $d_1, d_2$  with  $|d_1| = |d_2|$ .

If  $\text{TF}(t, d_1) > \text{TF}(t, d_2)$  then  $\rho(q, d_1) > \rho(q, d_2)$

Visualization:  $q$  

$d_1$  

$d_2$  

# Axiomatic Constraints for Retrieval Models

## Axiom Examples: TFC1 (practical)

Property: **Term frequency**

Intuition: Prefer documents with more occurrences of the query terms.

Formalization: Given a multi-term query  $q = \{t_1, \dots, t_n\}$  and two documents  $d_1, d_2$  with  $|d_1| \approx |d_2|$ .

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If  $\sum_{t \in q} \text{TF}(t, d_1) > \sum_{t \in q} \text{TF}(t, d_2)$  then  $d_1 >_{\text{TFC1}} d_2$

Visualization:  $q$  

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# Axiomatic Constraints for Retrieval Models

## Axiom Definitions

Property: <a “desirable” property>

Intuition: Prefer <documents> with <...>

Formalization: Given a <query>  $q$  and  
two <documents>  $d_1, d_2$  with <precondition>.

If <rule> then  $d_1 >_A d_2$

# Axiomatic Constraints for Retrieval Models

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## Remarks

- Simple if-then rules
  - Easy to explain axiom preferences
- Formal mathematical definition
  - Prove ranking model “errors” formally
  - Apply simple algorithms

# Axiomatic Constraints for Retrieval Models

## Axioms

### Term Frequency Constraints [Fang, Tao, Zhai 2004; 2011]

- TFC1 Prefer documents with more query term occurrences.
- TFC2 Additional query term occurrences yield smaller score improvements.
- TFC3 Prefer documents with occurrences of more distinct query terms.
- TDC Prefer documents with more discriminative query terms.

### Length Normalization Constraints [Fang, Tao, Zhai 2004]

- LNC1 Penalize longer documents for non-relevant terms.
- LNC2 Avoid over-penalizing long documents.
- TF-LNC Reward additional query terms more than document length is penalized.

### Lower-bounding Term Frequency Constraints [Lv and Zhai 2011]

- LB1 Do not override the term presence–absence gap with length normalization.
- LB2 Repeated query term occurrence is less important than first occurrence.

### Query Aspect-based Constr. [Gollapurdi and Sharma 2009; Zheng and Fang 2010; Wu and Fang 2012]

- REG Prefer documents covering more different query aspects.
- AND Prefer documents containing all query terms.
- DIV Prefer documents with larger vocabulary overlap with the query.

# Axiomatic Constraints for Retrieval Models

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### Semantic Similarity Constraints [Fang and Zhai 2006]

- STMC1 Prefer documents with terms more similar to query terms.
- STMC2 Do not reward similar terms more than exact matches.
- STMC3 Prefer documents with more distinct query terms

### Term Proximity Constraints [Tao and Zhai 2007; Hagen et al. 2016]

- PHC Prefer documents with query terms closer together.
- CCC Make the proximity-based score increase convex.
- PROX1 Prefer documents with shorter distance between query term pairs.
- PROX2 Prefer documents with earlier query term occurrences.
- PROX3 Prefer documents where the query occurs earlier as a phrase.
- PROX4 Prefer documents that contain all query terms in a shorter substring.
- PROX5 Prefer documents where the query terms are closer together on average.

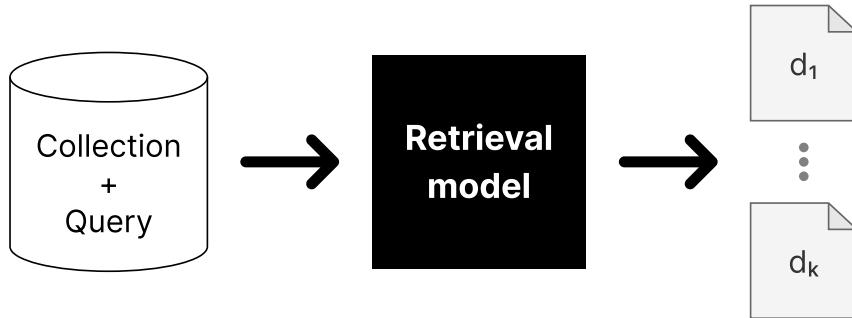
... and many more ...

# Axiomatic Information Retrieval Experimentation

- ❑ Axiomatic Constraints for Retrieval Models
- ❑ Applications for Retrieval Axioms
  - Overview
  - Explain Ranking Decisions
  - Axiomatic Re-Ranking
  - Axioms for RAG
- ❑ Hands-on: Axiomatic Experiments with `ir_axioms`
- ❑ Open Topics and Discussion

# Applications for Retrieval Axioms

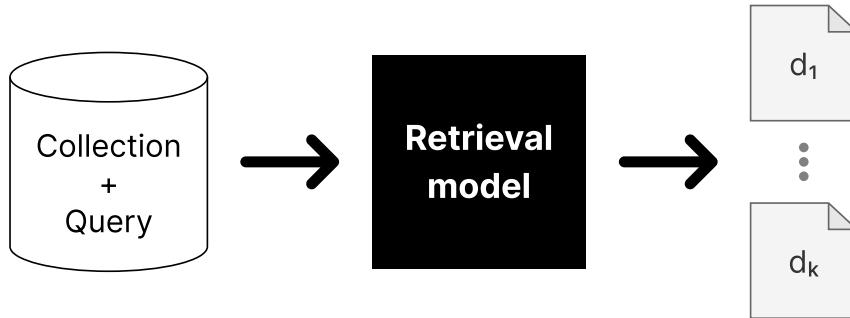
## Overview



- Analyze and explain neural rankers  
[Rennings et al. 2019; Camâra, Hauff 2020; Völske et al. 2021; Formal et al. 2021; MacAvaney et al. 2022]
- Improve effectiveness by re-ranking [Hagen et al. 2016]
- Improve (neural) model training [Rosset et al. 2019; Arora and Yates 2019]
- **New:** Analyze and explain RAG [Merker et al. 2025]

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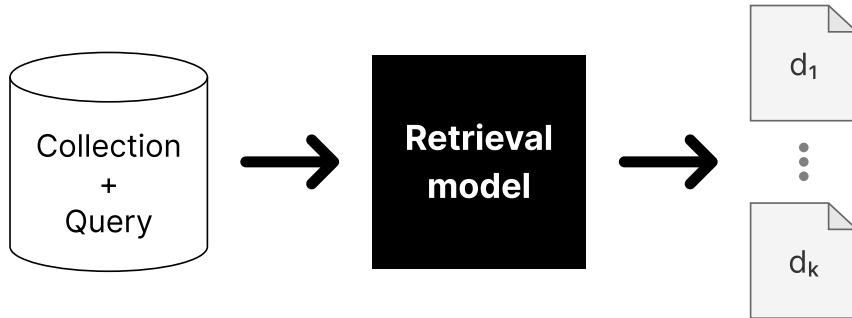
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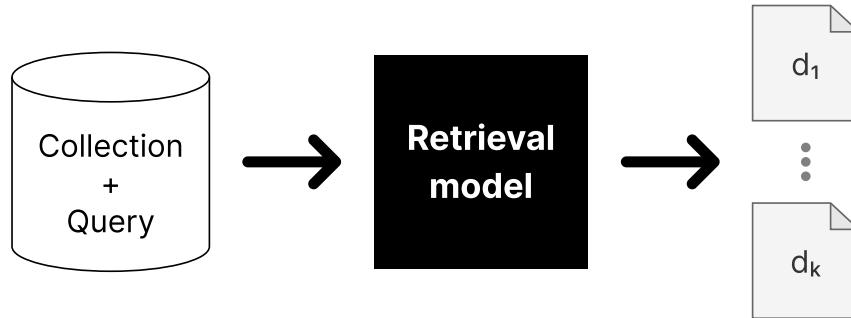
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- New: Analyze and explain RAG [Merker et al. 2025]
- How to run axiomatic experiments?

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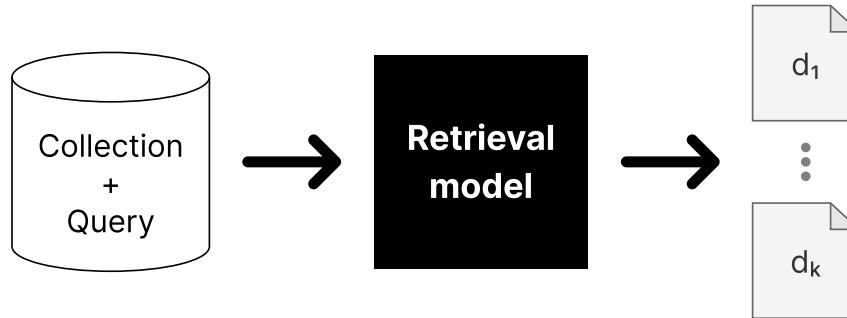
## Explain Ranking Decisions



- Many retrieval models too complex to interpret
- Do complex models still “obey” basic properties?

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## Axiomatic Relevance Hypothesis [Zhai and Fang 2013]

- Relevance modeled by constraints on retrieval function (i.e., axioms)
- System A satisfies many axioms → good effectiveness
- System A satisfies more than system B → system A better than B

**Approach:** Compare ranking preferences against axioms

# Applications for Retrieval Axioms

## Explain Ranking Decisions: Empirical Model

Prerequisite: Original ranking preferences [Hagen et al. 2016]

$$d_1 >_{\text{ORIG}} d_2 \Leftrightarrow \rho(q, d_1) > \rho(q, d_2)$$

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(applied to query  $q$  and ranking  $D = [d_1, \dots, d_n]$ )

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Example:

$$M_{\text{ORIG}} = \begin{bmatrix} 0 & 1 & 1 \\ -1 & 0 & 1 \\ -1 & -1 & 0 \end{bmatrix} \quad M_A = \begin{bmatrix} 0 & 1 & -1 \\ -1 & 0 & 1 \\ 1 & -1 & 0 \end{bmatrix}$$

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# Applications for Retrieval Axioms

## Explain Ranking Decisions

How often does a model satisfy the axiomatic constraints?

$$\text{Consistency}_A(q, D) = \frac{\sum_{i,j;j>i} M_{\text{ORIG}}[i, j] = M_A[i, j]}{(n^2 - n)/2}$$

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## Explain Ranking Decisions

Example:

$$\text{Consistency}_A(q, D) = \frac{2}{3} = 67\%$$

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# Applications for Retrieval Axioms

## Explain Ranking Decisions: TREC Deep Learning Track 2019

Step 1: Compare axiom consistency

Axiom	Documents			Passages		
	LLM	Neural	Trad.	LLM	Neural	Trad.
TFC1	48%	54%	66%	60%	56%	56%
STMC1	54%	52%	55%	57%	53%	55%
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Step 2: Debug individual violations (most effective run at TREC 2019 DL passage retrieval)

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### Step 3: Improve retrieval model based on findings → How?

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## Axiomatic Re-Ranking: Motivation

- BM25 (no matter the parameter setting) violates the LB2 constraint
- Minor modification corrects it → better effectiveness [Lv and Zhai 2011]

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$$\rho_{\text{BM25}}^+(q, d) = \sum_{t \in q} \text{IDF}(t) \cdot \left( \frac{\text{TF}(t, d) \cdot (k_1 + 1)}{\text{TF}(t, d) + k_1 \cdot \left(1 - b + b \cdot \frac{|d|}{\text{avgdl}}\right)} + \delta \right)$$

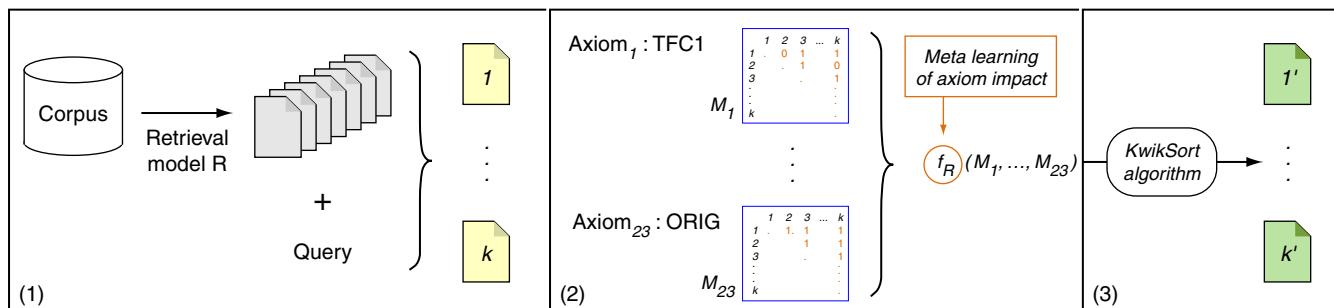
# Applications for Retrieval Axioms

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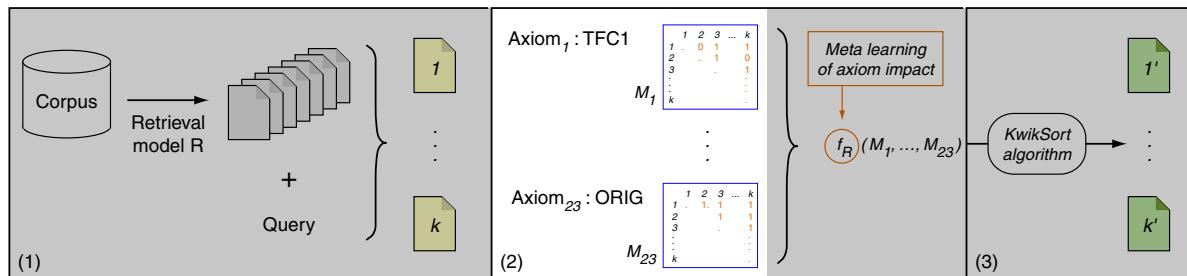
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→ Goal: Automate “axiomatization” of retrieval models with **axiomatic re-ranking**



# Applications for Retrieval Axioms

## Axiomatic Re-Ranking: Preference Matrices

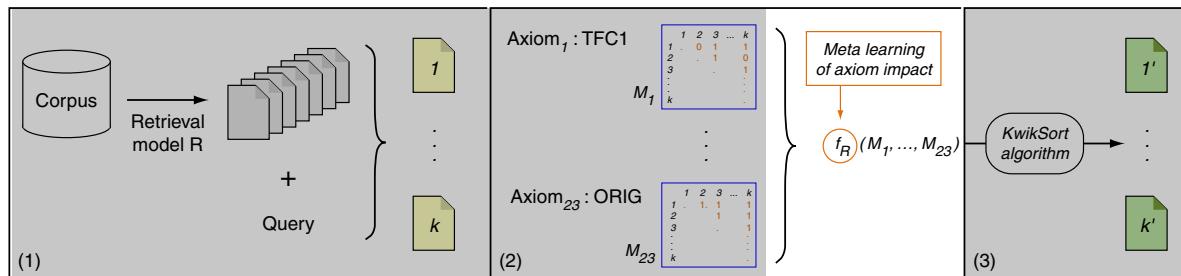


Step 1: From axioms and original ranking, compute preference matrices

$$\begin{array}{c} M_{\text{TFC1}} \quad M_{\text{PROX1}} \quad M_{\text{ORIG}} \\ \left[ \begin{array}{ccc} 0 & 1 & -1 \\ -1 & 0 & 1 \\ 1 & -1 & 0 \end{array} \right] \quad \left[ \begin{array}{ccc} 0 & 0 & 1 \\ -1 & 0 & 1 \\ 1 & -1 & 0 \end{array} \right] \quad \dots \quad \left[ \begin{array}{ccc} 0 & 1 & 1 \\ -1 & 0 & 1 \\ -1 & -1 & 0 \end{array} \right] \end{array}$$

# Applications for Retrieval Axioms

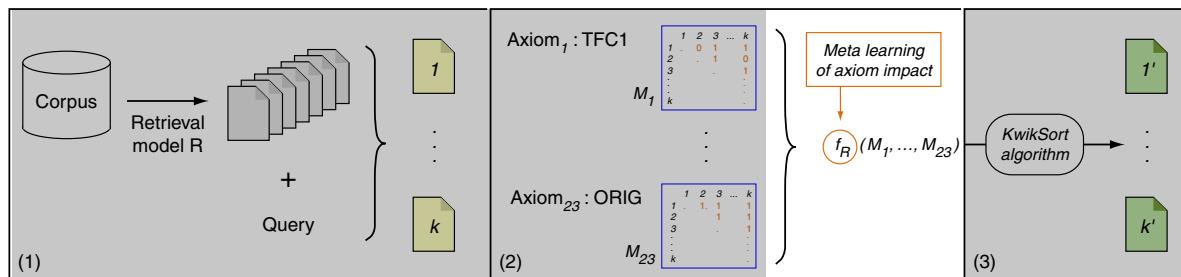
## Axiomatic Re-Ranking: Preference Aggregation



Step 2: Aggregate preference matrices to use aggregate preference for re-ranking.

# Applications for Retrieval Axioms

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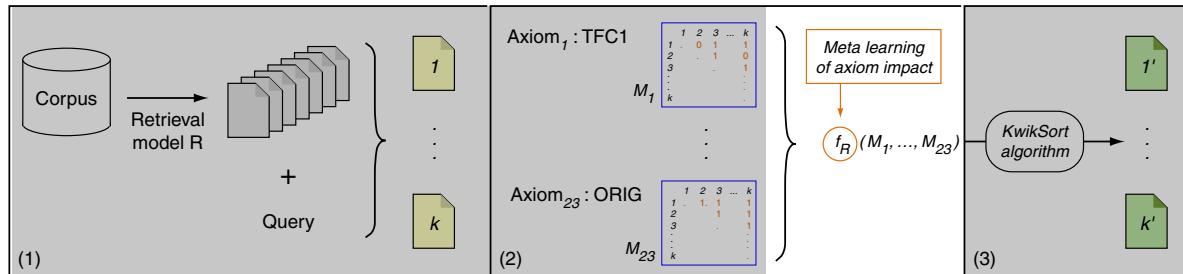


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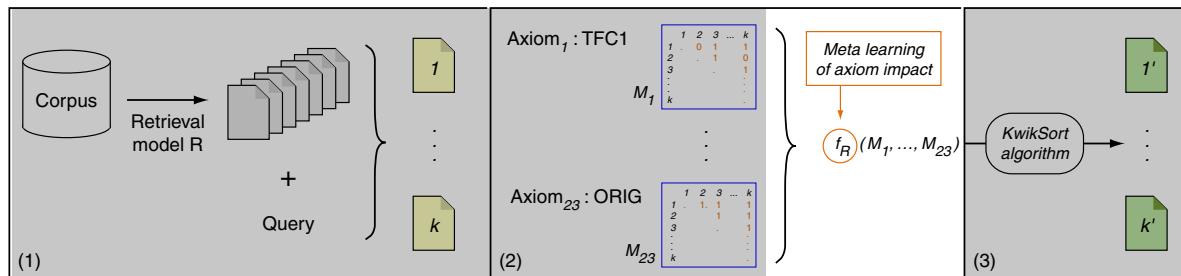
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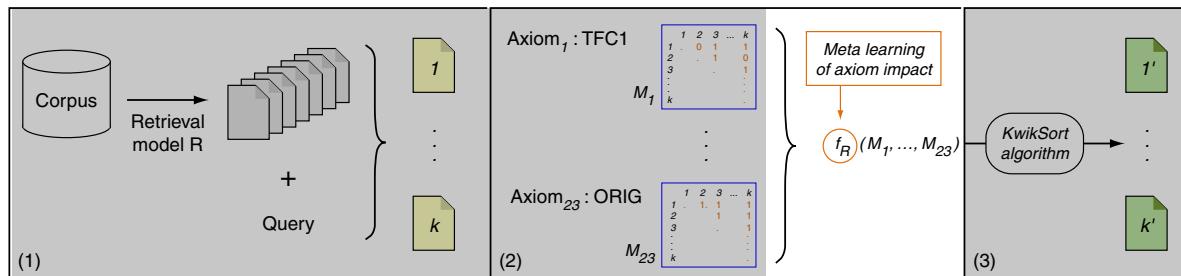
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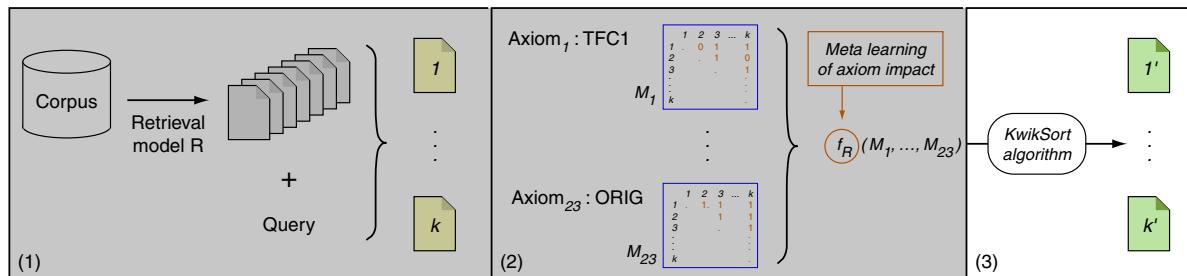
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# Applications for Retrieval Axioms

## Axiomatic Re-Ranking: KwikSort



Step 3: From aggregated preference matrix, derive final ranking.

- Aggregated preference matrix can contain contradictions, e.g.  $M[i, j] = M[j, i]$
- Rank-aggregation to resolve contradictions [Kemeny 1959]
- Algorithm: KwikSort [Ailon, Charikar, Newman 2008]  
(works similar to QuickSort)

# Applications for Retrieval Axioms

## RAG Axioms: Motivation

- Problem: Utility of RAG responses not just topical relevance
- Ground-truth-based evaluation
- Ground-truth-free approaches



# Applications for Retrieval Axioms

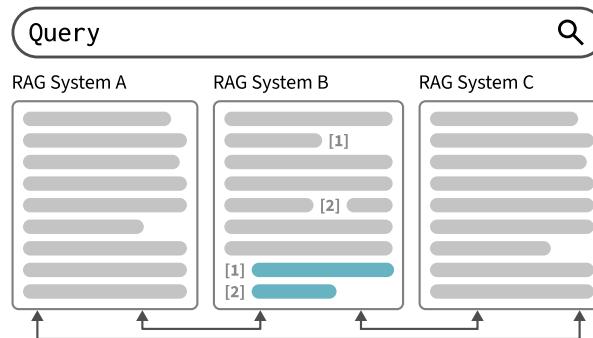
## RAG Axioms: Motivation

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  - Information nuggets: SWAN, LLM-Rubric, TREC RAG
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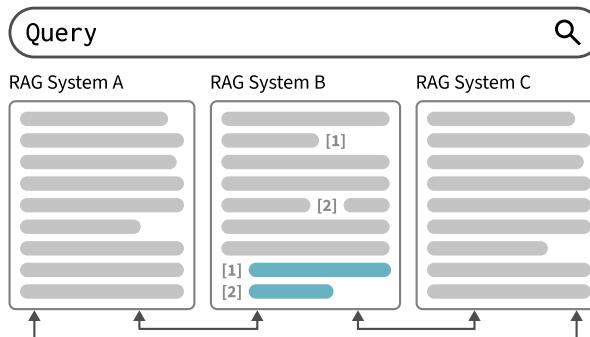
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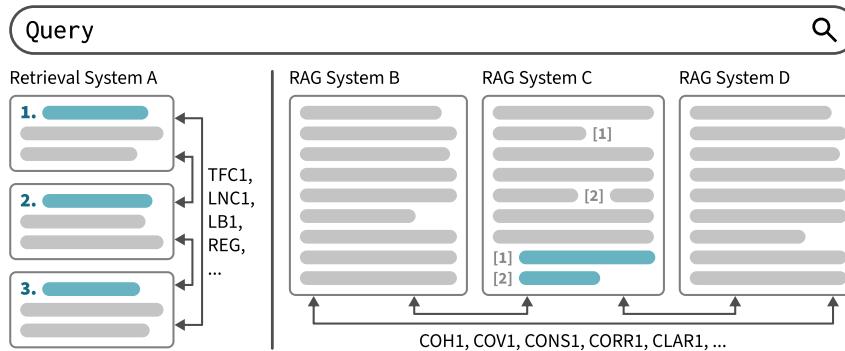
## Limitations

- Scalability: Cost of manual judgments (or LLM inference)
- Explainability: Opaque, biased LLMs used in evaluation

# Applications for Retrieval Axioms

## RAG Axioms: Approach

- Traditional axioms: “Vertical” preferences on a single system’s ranking
- RAG axioms: “Horizontal” preferences between different systems



## Adapt Traditional Axioms

- Reuse from `ir_axioms`
- Limitation: index statistics for “infinite index”
- 18 of 25 traditional axioms adapted for RAG

## New RAG-specific Axioms

- Utility dimensions [Gienapp et al. 2024]: Coherence, correctness, coverage, consistency, clarity
- 11 new RAG axioms
- Integrated into `ir_axioms`

# Applications for Retrieval Axioms

## RAG Axioms

### Coherence-based Constraints

- COH1 Prefer responses with less variance in **avg. word length** across sentences.
- COH2 Prefer responses with **subject–verb pairs** closer together.

### Coverage-based Constraints

- COV1 Prefer responses with more **extracted aspects** in response.
- COV2 Prefer responses with **less redundant** extracted aspects.
- COV3 Prefer responses with more sentences covering **aspects from the query**.

### Consistency-based Constraints

- CONS1 Prefer responses with more sentences covering **aspects from the context**.
- CONS2 Prefer responses with higher **text overlap** with contexts.
- CONS3 Penalize aspects mentioned in **contradictory phrases**.

### Correctness-based Constraints

- CORR1 Prefer responses with more sentences with **references** to sources.

### Clarity-based Constraints

- CLAR1 Prefer responses with fewer **grammar errors**.
- CLAR2 Prefer responses with better **readability**.

**... not complete** → Contribute!

# Applications for Retrieval Axioms

## RAG Axioms: Experiments

- TREC 2025 RAG: Information nuggets recall / coverage → LLM-based
- Webis CrowdRAG-25: Crowd-sourced judgments, 5 utility dims. → Manual

## Method

- Consistency with oracle preferences
- Decisiveness (How often does the axiom yield a preference?)
- Use cases: [Inspect LM generation preferences](#), aid annotation, etc.

Query	good morning accenture	TFC <sup>1</sup>	STM <sup>1</sup>	PROX <sup>2</sup>	PROX <sup>3</sup>	PROX <sup>4</sup>	PROX <sup>5</sup>	COH <sup>1</sup>	COV <sup>1</sup>	COV <sup>2</sup>	COV <sup>3</sup>	CONS <sup>1</sup>	CONS <sup>2</sup>	CORR <sup>1</sup>	CORR <sup>2</sup>	CLAR <sup>2</sup>
# Response		✓	✓	✓	✗	✓	✓	✓	✗	✗	✗	✗	✗	✓	✗	✓
1	"The question can't be answered using the references provided. Please try with shorter phrases [...] to find out relevant results."	✓	✓	✓	✗	✓	✓	✓	✗	✗	✗	✗	✗	✓	✗	✓
2	"The "Good Morning Accenture" initiative [...] has significantly impacted the company by repositioning and invigorating [...] consultation and technological advancement [3, 4]."	✗	✗	✗	✓	✗	✗	✗	✓	✓	✓	✓	✓	✓	✗	✓

# Axiomatic Information Retrieval Experimentation

- ❑ Axiomatic Constraints for Retrieval Models
- ❑ Applications for Retrieval Axioms
- ❑ Hands-on: Axiomatic Experiments with `ir_axioms`
  - The `ir_axioms` Framework
  - Post-hoc Axiomatic Analyses
  - Axiomatic Re-Ranking
  - Developing New Retrieval Axioms
- ❑ Open Topics and Discussion

# Hands-on: Axiomatic Experiments with `ir_axioms`

## Practical Axiomatic Experiments

- Many IR toolkits: Terrier, Anserini, etc.
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## The `ir_axioms` Framework

- ❑ Python library adds axiom components to IR toolkits
- ❑ 25 retrieval axioms and 11 RAG axioms included with practical relaxations, e.g.,  $|d_1| \approx_{10\%} |d_2|$  for TFC1
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## Design Goals

1. Usable: Supports many axiomatic applications
2. Extensible: Easy to define new axioms  
... by extending a Python class
3. Composable: “Remix” axioms to build more complex constraints  
... by using Python operators

# Hands-on: Axiomatic Experiments with `ir_axioms`

## Showcase

Jupyter Notebook:

[https://github.com/webis-de/ir\\_axioms/blob/main/experiments/grenoble2025\\_showcase.ipynb](https://github.com/webis-de/ir_axioms/blob/main/experiments/grenoble2025_showcase.ipynb)

# Hands-on: Axiomatic Experiments with `ir_axioms`

## Developing New (Retrieval) Axioms

Recall: Axiom Definitions

Property: <a “desirable” property>

Intuition: Prefer <documents> with <...>

Formalization: Given an <input>  $q$  and  
two <documents>  $d_1, d_2$  with <precondition>.  
If <rule> then  $\rho(q, d_1) > \rho(q, d_2)$

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Steps to develop an axiom:

1. Identify desirable property
2. Formalize as pairwise preference between two documents
3. Implement the axiom in `ir_axioms`
4. Run experiments

# Axiomatic Information Retrieval Experimentation

## Summary

- Formally analyze and explain retrieval and RAG
- More than 30 axioms implemented in `ir_axioms`
  - Post-hoc analyses
  - Axiomatic re-ranking
  - Easy to define new axioms
- Axioms **support** not **replace** typical evaluation

Software and examples → Contributions are welcome!

Code

- ⌚ [webis-de/ir\\_axioms](https://github.com/webis-de/ir_axioms)
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Future Work: More axioms for RAG, other domains/modalities, regularize LLM's, ...

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